# Analysis of Axial Field Magnetic Gears with Halbach Arrays

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Abstract-- Magnetic gears can scale the torque and speed of rotary systems, while avoiding problems associated with transferring torque through physical contact. This work uses 3D finite element analysis to parametrically characterize the performance benefits which can be obtained from applying Halbach magnet arrays to axial field magnetic gears. It is found that Halbach arrays decrease the flux density in the adjacent back iron, allowing the thickness of these yokes to be reduced. Also, using Halbach arrays increases the magnitude of the desired magnetic flux spatial frequencies in the air gaps, increasing torque, and decreases the magnitude of undesired spatial frequencies, decreasing torque ripple. Additionally, the use of Halbach arrays on both rotors increased the torque volumetric torque density for two different design points by 43.6% and 65.7% to 183.9 and 155.8 kN\*m/m<sup>3</sup>, respectively, and decreased the cogging torque on both rotors.

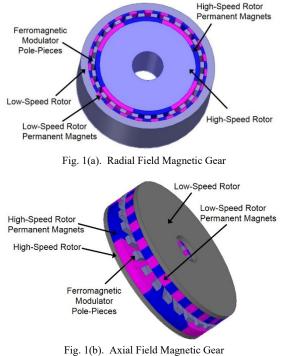
*Index Terms*—Axial flux, finite element analysis, Halbach arrays, hermetic isolation, magnetic gear, torque ripple

### I. INTRODUCTION

MAGNETIC gears are a technology that has garnered significant attention in recent years [1]-[4] due to their potential to offer a plethora of advantages over mechanical gears. Like their mechanical counterparts, magnetic gears can be used to scale up and down the torque and speed of rotary systems. However, magnetic gears transfer torque through the modulated interaction of magnetic fields rather than through mechanical teeth. This results in the potential for higher reliability, lower acoustic noise, increased efficiency, and physical isolation between shafts.

Magnetic gears have been proposed for several industrial applications. For wind energy generation, magnetic gears can transform the high torque, low speed rotation of the turbine to a low torque, high speed input for the generator, allowing a significantly smaller generator to be used, without the maintenance required for a mechanical gear [2]. Conversely, in traction applications, such as electric vehicles, a magnetic gear can transform the low torque, high speed rotation of a motor into the required high torque, low speed output, enabling a smaller motor and smaller total system volume and mass [3]. Similarly, magnetic gears have been designed for underwater propulsion, where reduced acoustic noise is critically important [4].

Most of the previous work on magnetic gears has focused on the radial field topology shown in Fig. 1(a). However, recently interest has increased in the axial field topology [5]-[7] shown in Fig. 1(b), despite its additional difficulties in construction, because it can easily be used in situations requiring hermetic isolation. Two methods that have been used to increase the torque density of magnetic gear designs are flux-focusing permanent magnet configurations and Halbach arrays. Flux-focusing arrangements have been applied to both radial [8] and axial [6] field topologies, resulting in high torque densities. The use of Halbach magnetic arrays has been applied to radial field magnetic gears to improve torque density and reduce torque ripple [9]-[11]. However, to the authors' knowledge, Halbach arrays have not been applied to axial field magnetic gears. This study employs parametric 3D finite element (FE) simulations to analyze the benefits obtained by incorporating Halbach arrays into axial field magnetic gears.



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#### II. AXIAL FIELD HALBACH CONFIGURATIONS

The permanent magnet (PM) arrays in a conventional axial field gear consist of magnet pieces with alternating "upward" and "downward" magnetizations, denoted by the blue and purple magnets in Fig. 1(b). Alternatively, an axial Halbach array consists of N<sub>P</sub> magnet pieces per pole, with the k<sup>th</sup> piece having a magnetization angle,  $\gamma_k$ , given by (1) in radians. The individual magnet pieces have both axial and tangential magnetization components which are determined based on  $\gamma_k$  according to (2) and (3). In this manner, a traditional axial field magnetic gear can be viewed as a specific, albeit crude, Halbach configuration with N<sub>P</sub> set to 1 for both the high speed rotor (rotor 1) and the low speed rotor (rotor 2) (N<sub>P1</sub> = 1 and N<sub>P2</sub> = 1).

$$\gamma_{k} = \left(\frac{\pi}{2}\right) \pm \left(\frac{k-1}{N_{p}}\right) \times \pi \tag{1}$$

$$\mathbf{M}_{\mathbf{k},\mathbf{z}} = \left| \mathbf{M} \right| \times \sin(\gamma_{\mathbf{k}}) \tag{2}$$

$$\mathbf{M}_{\mathbf{k},\theta} = \left| \mathbf{M} \right| \times \cos\left( \gamma_{\mathbf{k}} \right) \tag{3}$$

A Halbach magnet array, such as the one shown in Fig. 2, creates a more sinusoidal field distribution on one side of the array, while decreasing the field intensity on the other side in a phenomenon known as self-shielding [9]. The " $\pm$ " sign in (1) is selected as a "+" or a "-" to control the side of the array (top or bottom) on which the field is concentrated. The Halbach array shown in Fig. 2, with N<sub>P</sub> = 3, produces a pseudo-sinusoidal axial field distribution on its z- side.

Increasing the value of  $N_P$  in a Halbach array reduces harmonics in the sinusoidal field distribution on one side while further reducing the field intensity on the other. This can enhance magnetic gear designs by increasing the stall torque, reducing the torque ripple, reducing the requisite amount of back iron material, and improving efficiency. As with traditional (non-Halbach) magnetic gears, the number of pole pairs on rotor 1,  $P_{PM1}$ , the number of pole pairs on rotor 2,  $P_{PM2}$ , and the number of modulator pieces,  $Q_M$ , are still related by (4) resulting in the gear ratio given by (5).

$$Q_{\rm M} = P_{\rm PM1} + P_{\rm PM2} \tag{4}$$

$$G_{\rm r} = \frac{\omega_{\rm rotor1}}{\omega_{\rm rotor2}} = \frac{-P_{\rm PM2}}{P_{\rm PM1}}$$
(5)



Fig. 2. Halbach Magnet Array (with  $N_P = 3$ ) Focusing the Magnetic Field Below the Array (in the z- Direction)

#### III. DEFINITION OF KEY DESIGN PARAMETERS

A fully parameterized 3D finite element analysis (FEA) model was developed in ANSYS Maxwell to investigate the impact of various design variables on the axial field magnetic gear's performance with and without Halbach arrays. A summary of the most important parameters is provided in Table I. For all design points presented in this study, both air gap thicknesses were fixed at 2 mm and the modulator thickness was held constant at 10 mm.

In an effort to reduce the dimensionality of the parametric design space, three interconnecting design parameters,  $K_{BII}$ ,  $K_{BI2}$ , and  $G_r$ , were each developed to set one design variable as a dependent function of another design variable. Descriptions of these parameters are provided in Table 1 and their mathematical definitions are given in (6) – (8). In particular, the  $G_r$  parameter and the associated relationship given by (8) were employed to ensure that all design points used pole pair combinations with relatively large least common multiples (LCMs), which is crucial for achieving low torque ripple performance [2].

TABLE I Descriptions of Basic Design Parameters

Parameter	Description		
P <sub>PM1</sub>	Rotor 1 magnetic pole pairs		
P <sub>PM2</sub>	Rotor 2 magnetic pole pairs		
Gr	Closest integer gear ratio not exceeding the actual gear ratio.		
-	Floor(Gear Ratio)		
N <sub>P1</sub>	Rotor 1 magnet pieces per pole		
N <sub>P2</sub>	Rotor 2 magnet pieces per pole		
R <sub>1</sub>	Axial gear inner radius		
R <sub>2</sub>	Axial gear outer radius		
T <sub>PM1</sub>	Axial thickness of the rotor 1 magnets		
T <sub>PM2</sub>	Axial thickness of the rotor 2 magnets		
T <sub>AG</sub>	Axial thickness of both air gaps		
T <sub>Mods</sub>	Axial thickness of the modulators		
k <sub>BI1</sub>	Ratio of the rotor 1 back iron and		
	magnet axial thicknesses		
$k_{\rm BI2}$	Ratio of the rotor 2 back iron and		
	magnet axial thicknesses		

$$k_{BI1} = \left(\frac{\text{Rotor 1 Back Iron Thickness}}{\text{Rotor 1 Magnet Thickness}}\right)$$
(6)

$$k_{BI2} = \left(\frac{\text{Rotor 2 Back Iron Thickness}}{\text{Rotor 2 Magnet Thickness}}\right)$$
(7)

$$P_{PM2} = G_r \times P_{PM1} + 1 \tag{8}$$

## IV. BACK IRON FLUX DENSITY STUDIES

The self-shielding effect of Halbach arrays can be used to significantly decrease the flux density in the magnetic gear's back irons. In turn, this can be used to build a smaller, lighter gear while maintaining performance ratings and even decreasing losses (especially since the arrays also decrease harmonic amplitudes). To quantify this effect, the rotor 1 back iron thickness was held constant while the rotor 1 Habach number (N<sub>P1</sub>) was swept from 1 to 4 at different rotor 1 pole pair values and the resulting maximum back iron 1 (BI<sub>1</sub>) flux densities are depicted in Fig. 3. A similar analysis is shown for rotor 2 in Fig. 4. Both studies were conducted at  $G_r = 4$  design points. For each parametric graph presented in this study, the values of pertinent design parameters which were held constant in the corresponding analysis are provided in the graph's caption.

The results in Fig. 3 and Fig. 4 demonstrate that the back iron flux densities can be significantly reduced by the use of Halbach arrays, with the largest improvements observed in the transition from  $N_P = 1$  to  $N_P = 2$  on either rotor. As the  $N_P$  value is increased beyond 2, the back iron flux densities continue to decrease at a slower rate. Thus, the value of these diminishing returns must be weighed against the increased manufacturing complexity.

Furthermore, a comparison of the data for the two rotors reveals that increasing  $N_{P1}$  has a much more profound impact on the rotor 1 back iron flux density than increasing  $N_{P2}$  has on the rotor 2 back iron flux density. This is due in part to the fact that rotor 2 already inherently has more pole pairs than rotor 1, in accordance with the gear ratio, and thus has shorter tangential flux paths. The higher pole pair count on rotor 2 also imposes the practical limitation that  $N_{P2}$  should be restricted to a smaller range of values than  $N_{P1}$  because of manufacturing complexity considerations.

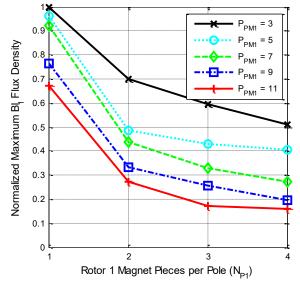


Fig. 3. Rotor 1 Maximum Back Iron Flux Density Variation with Rotor 1 Magnet Pieces per Pole (N<sub>P1</sub>). Fixed Values: (N<sub>P2</sub> = 1; k<sub>B11</sub> = 1; k<sub>B12</sub> = 1; T<sub>PM1</sub> = 12.7 mm; T<sub>PM2</sub> = 6.35 mm; R<sub>1</sub> = 100 mm; R<sub>2</sub> = 167 mm; G<sub>r</sub> = 4).

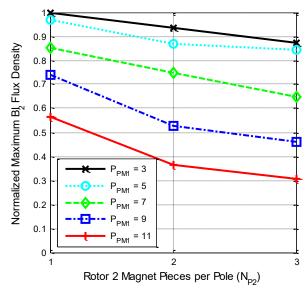


Fig. 4. Rotor 2 Maximum Back Iron Flux Density Variation with Rotor 2 Magnet Pieces per Pole (N<sub>P2</sub>). Fixed Values: (N<sub>P1</sub> = 1; k<sub>B11</sub> = 1; k<sub>B12</sub> = 1; T<sub>PM1</sub> = 12.7 mm; T<sub>PM2</sub> = 6.35 mm; R<sub>1</sub> = 100 mm; R<sub>2</sub> = 167 mm; G<sub>r</sub> = 4).

The impact of the Halbach arrays on the back iron flux densities was also examined by sweeping the back iron thicknesses at different Halbach numbers with all other design parameters held constant. The results are shown for rotor 1 in Fig. 5 and rotor 2 in Fig. 6. The graph in Fig. 5 reveals that using a Halbach array on rotor 1 can achieve back iron flux density reductions comparable to those obtained by tripling the rotor 1 back iron thickness. The plot in Fig. 6 shows that although the rotor 2 Halbach self-shielding effect is not as significant as seen on rotor 1, it can still result in back iron flux density reductions comparable to those achieved by a 50% increase in the rotor 2 back iron thickness.

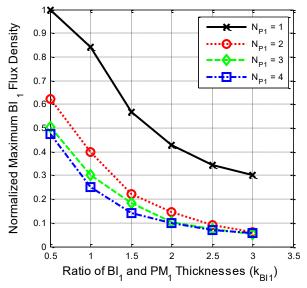


Fig. 5. Rotor 1 Maximum Back Iron Flux Density Variation with Rotor 1 Back Iron Thickness Ratio. Fixed Values:  $(N_{P2} = 1; P_{PM1} = 7; k_{B12} = 1; T_{PM1} = 12.7 \text{ mm}; T_{PM2} = 6.35 \text{ mm}; R_1 = 100 \text{ mm}; R_2 = 167 \text{ mm}; G_r = 4).$ 

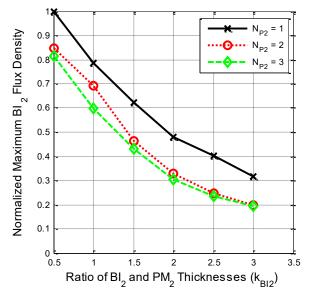


Fig. 6. Rotor 2 Maximum Back Iron Flux Density Variation with Rotor 2 Back Iron Thickness Ratio. Fixed Values:  $(N_{P1} = 1; P_{PM1} = 7; k_{B11} = 1; T_{PM1} = 12.7 \text{ mm}; T_{PM2} = 6.35 \text{ mm}; R_1 = 100 \text{ mm}; R_2 = 167 \text{ mm}; G_r = 4).$ 

#### V. AIR GAP FLUX DENSITY STUDIES

The effects of the Halbach arrays on the air gap axial flux densities were also examined for a 28:3 gear ( $P_{PM1} = 3$ ,  $P_{PM2} = 28$ ). Fig. 7 shows an FFT analysis of the axial flux density in the air gap adjacent to rotor 2 with only the rotor 1 magnets and the modulators included in the system. Similarly, Fig. 8 shows an FFT analysis of the axial flux density in the air gap adjacent to rotor 1 with only the rotor 2 magnets and the modulators in the system. These graphs illustrate that the Halbach arrays significantly increase the amplitude of the

desired spatial harmonics while also reducing the amplitude of most of the undesired harmonics. This leads to designs with higher stall torque and reduced torque ripple.

#### VI. TORQUE DENSITY AND AXIAL FORCE STUDIES

In addition to the flux density studies, the Halbach arrays were also evaluated for their effects on the torque ratings of different axial field magnetic gear designs. As with the back iron flux density studies, the impacts of the Halbach arrays on both rotors were evaluated separately. Fig. 9 and Fig. 11 show the impact of the rotor 1 and rotor 2 Halbach arrays on the axial field magnetic gear's volumetric torque density at  $G_r = 4$  design points with different numbers of poles. Fig. 10 and Fig. 12 show the magnitudes of the corresponding axial forces. From these figures, it is evident that increasing the Halbach number on either rotor increases torque density, at the expense of increased axial forces, which necessitate increased structural support. Additionally, these figures show that the effects of increasing the Halbach number decrease at higher values. Due to these diminishing returns, as well as the manufacturing difficulties induced by increasing Halbach numbers, designs with  $N_{P1} = 3$  and  $N_{P2} =$ 2 were chosen for further simulation comparison with  $N_{P1}$  = 1 and  $N_{P2}$  = 1 (non-Halbach array) design points. The Halbach array and non-Halbach array gears were compared at both Gr = 4 and Gr = 9 design points. The other values of the parameters are provided in Table II for Gr values of 4 and 9. The resulting volumetric torque densities are given in Table III. This shows a 43.6% increase in torque density for  $G_r = 4$  and a 65.7% increase in torque density for  $G_r = 9$ .

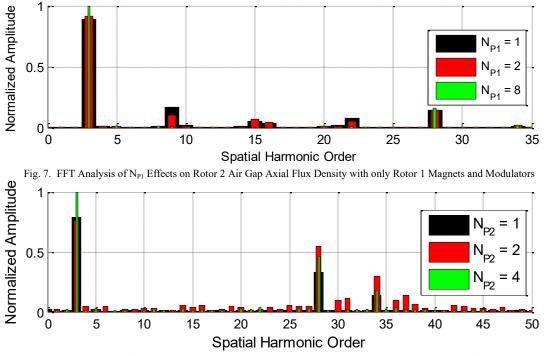


Fig. 8. FFT Analysis of N<sub>P2</sub> Effects on Rotor 1 Air Gap Axial Flux Density with only Rotor 2 PMs and Modulators

Parameter	Value for Gr = 4	Value for Gr = 9
P <sub>PM1</sub>	7	5
P <sub>PM2</sub>	29	46
R <sub>1</sub>	100 mm	100 mm
R <sub>2</sub>	167 mm	167 mm
T <sub>PM1</sub>	12.7 mm	12.7 mm
T <sub>PM2</sub>	6.35 mm	6.35 mm
T <sub>AG</sub>	2 mm	2 mm
T <sub>Mods</sub>	10 mm	10 mm
k <sub>BI1</sub>	0.5	0.5
k <sub>BI2</sub>	0.5	0.5

TABLE II Values of Design Parameters

TABLE III Volumetric Torque Density Results

Volumetric Torque Density (kN*m/m <sup>3</sup> )	$\begin{split} \mathbf{N}_{P1} &= 1\\ \mathbf{N}_{P2} &= 1 \end{split}$	$\begin{array}{l} N_{P1}=3\\ N_{P2}=2 \end{array}$
$G_r = 4$	128.1	183.9
$G_r = 9$	94.0	155.8

Fig. 13 and Fig 14. show the effects of the back iron thicknesses on the torque density for different Halbach numbers. This data demonstrates that increasing  $N_{P1}$  and  $N_{P2}$  significantly improves volumetric torque density for thin back irons because they become saturated easily, but the self-shielding effect of the Halbach array decreases the flux density passing through the back irons. For higher back iron thicknesses, there is no danger of saturation, which reduces the benefit of increasing the Halbach number. Both figures also indicate that maximum torque density is achieved with no back iron for  $N_P$  greater than 1. These air core design points deserve further study, as they offer excellent torque density, but present other difficulties, such as structural support and magnetic containment.

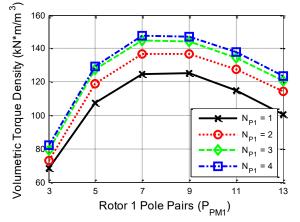


Fig. 9. Volumetric Torque Density Variation with Rotor 1 Pole Pairs for Different Rotor 1 Halbach Configurations at  $G_r = 4$ . Fixed Values: ( $N_{P2} = 1$ ;  $k_{B11} = 0.5$ ;  $k_{B12} = 1$ ;  $T_{PM1} = 12.7$  mm;  $T_{PM2} = 6.35$  mm;  $R_1 = 100$  mm;  $R_2 = 167$  mm;  $G_r = 4$ ).

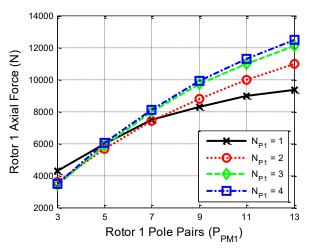


Fig. 10. Impact of Rotor 1 Pole Pairs on Rotor 1 Axial Force for Different Rotor 1 Halbach Configurations at  $G_r = 4$ . Fixed Values: ( $N_{P2} = 1$ ;  $k_{B11} = 0.5$ ;  $k_{B12} = 1$ ;  $T_{PM1} = 12.7$  mm;  $T_{PM2} = 6.35$  mm;  $R_1 = 100$  mm;  $R_2 = 167$  mm;  $G_r = 4$ ).

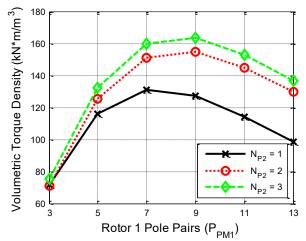


Fig. 11. Volumetric Torque Density Variation with Rotor 1 Pole Pairs for Different Rotor 2 Halbach Configurations at  $G_r = 4$ . Fixed Values: ( $N_{P1} = 1$ ;  $k_{B11} = 1$ ;  $k_{B12} = 0.5$ ;  $T_{PM1} = 12.7$  mm;  $T_{PM2} = 6.35$  mm;  $R_1 = 100$  mm;  $R_2 = 167$  mm;  $G_r = 4$ ).

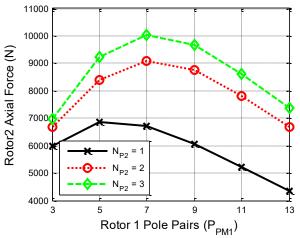


Fig. 12. Impact of Rotor 1 Pole Pairs on Rotor 2 Axial Force for Different Rotor 2 Halbach Configurations at  $G_r = 4$ . Fixed Values: ( $N_{P1} = 1$ ;  $k_{B11} = 1$ ;  $k_{B12} = 0.5$ ;  $T_{PM1} = 12.7$  mm;  $T_{PM2} = 6.35$  mm;  $R_1 = 100$  mm;  $R_2 = 167$  mm;  $G_r = 4$ ).

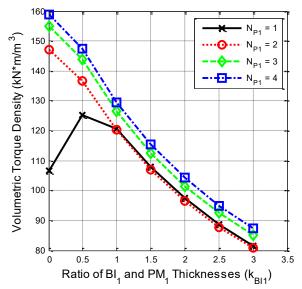


Fig. 13. Volumetric Torque Density Variation with Rotor 1 Back Iron Thickness Ratio. Fixed Values: ( $N_{P2} = 1$ ;  $P_{PM1} = 9$ ;  $k_{B12} = 1$ ;  $T_{PM1} = 12.7$  mm;  $T_{PM2} = 6.35$  mm;  $R_1 = 100$  mm;  $R_2 = 167$  mm;  $G_r = 4$ ).

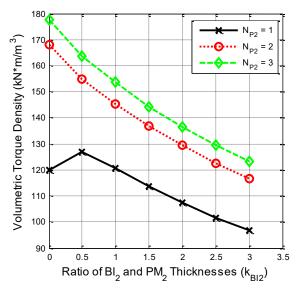


Fig. 14. Volumetric Torque Density Variation with Rotor 2 Back Iron Thickness Ratio. Fixed Values: (N<sub>P1</sub> = 1; P<sub>PM1</sub> = 9; k<sub>B11</sub> = 1; T<sub>PM1</sub> = 12.7 mm; T<sub>PM2</sub> = 6.35 mm; R<sub>1</sub> = 100 mm; R<sub>2</sub> = 167 mm; G<sub>r</sub> = 4).

#### VII. COGGING TORQUE STUDIES

The same design points listed in Table II were also evaluated to determine their respective levels of torque ripple at different loads. The results are shown in Fig. 15 for the rotor 1 torque and Fig. 16 for the rotor 2 torque. The load is represented by the electromagnetic torque angle, which describes the relative electromagnetic angular position of the two rotors. An electromagnetic torque angle of 90 degrees corresponds to maximum torque transmission and a torque angle of 0 degrees ideally corresponds to no torque transmission. This data clearly illustrates that the Halbach arrays reduce the torque ripple on both rotors for both gear ratio designs by 50-75%. This reduction in cogging torque is a result of the trends discussed in the air gap flux density study. The Halbach arrays significantly increase the amplitude of the fundamental air gap flux density component relative to the undesirable harmonic air gap flux density components which produce the torque ripple.

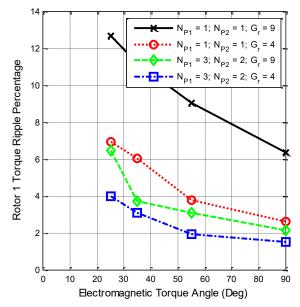


Fig. 15. Variation of Rotor 1 Torque Ripple with Torque Angle for Halbach Array and non-Halbach Array Designs. Fixed Values: ( $k_{BI1} = 0.5$ ;  $k_{BI2} = 0.5$ ;  $T_{PM1} = 12.7$  mm;  $T_{PM2} = 6.35$  mm;  $R_1 = 100$  mm;  $R_2 = 167$  mm).

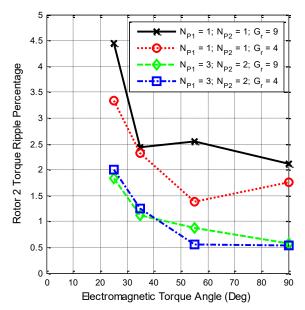


Fig. 16. Variation of Rotor 2 Torque Ripple with Torque Angle for Halbach Array and non-Halbach Array Designs. Fixed Values: ( $k_{BII} = 0.5$ ;  $k_{BI2} = 0.5$ ;  $T_{PMI} = 12.7$  mm;  $T_{PM2} = 6.35$  mm;  $R_1 = 100$  mm;  $R_2 = 167$  mm).

#### VIII. CONCLUSION

The arrangement of the permanent magnets into Halbach arrays for an axial field magnetic gear was proposed and analyzed. Parametric FEA simulations were run to analyze trends related to the Halbach numbers and other design parameters of the magnetic gear topology. It was shown that implementing Halbach arrays decreased the magnetic flux density in the back irons, which can decrease losses and allow for thinner back irons. Additionally, with the implementation of Halbach arrays, the desirable harmonics of the magnetic flux density in the air gaps increased, while the undesirable harmonics decreased. Volumetric torque density and axial forces were shown to increase with Halbach number.

Based on the results of several trends, design points were picked for further simulation. For a gear ratio of 4.14, it was shown that using Halbach arrays on both rotors could elevate the torque density from 128.1 kN\*m/m<sup>3</sup> to 183.9 kN\*m/m<sup>3</sup>, an increase of 43.6%. For a gear ratio of 9.2, using Halbach arrays on both rotors raised the torque from 94.0 kN\*m/m<sup>3</sup> to 155.8 kN\*m/m<sup>3</sup>, an increase of 65.7%. Finally, it was demonstrated that the Halbach arrays lowered the torque ripple on both rotors under several different load conditions. Thus, Halbach arrays can significantly improve the performance of axial field magnetic gears.

### IX. ACKNOWLEDGMENT

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#### XI. BIOGRAPHIES

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